

Structure-aware bottle cap art

Leonardo Sacht

UFSC

SIBGRAPI 2022 / C&G paper

Motivation: plastic bottle caps



Image source: diveagainstdebris.org

- Long time to degenerate.
- Small to be mistaken for food by sea animals.

Motivation: plastic bottle caps



Image source: diveagainstdebris.org

- Long time to degenerate.
- Small to be mistaken for food by sea animals.
- Top 5 ocean trash items that are deadly for sea life (North Sea Foundation, 2017).

Motivation: low resolution images



Source: pngitem.com



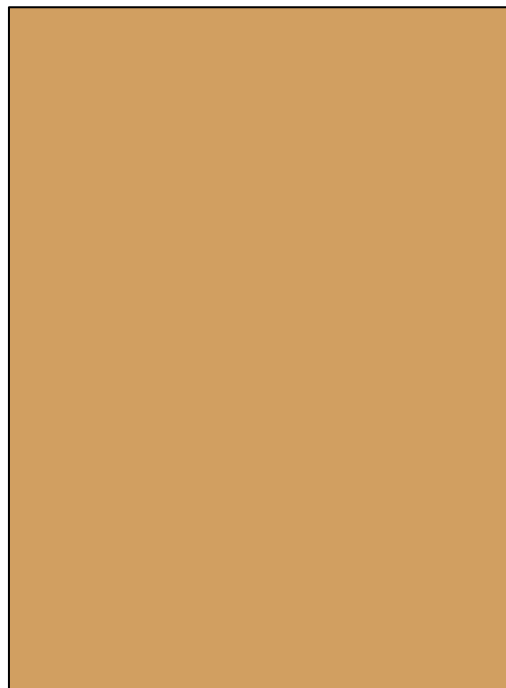
Source: la-boite-a-trouvailles.com



Source: flickr.com

Contributions

- 1191
- 580
- 414
- 360
- 337
- 234
- 195
- 110
- 90
- 73



New image
processing
problem

Caps

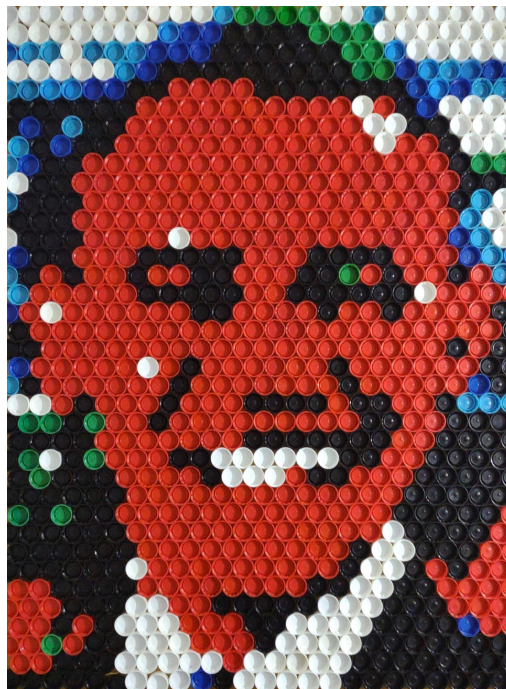
Input image

Canvas

Source: whitehouse.gov

Contributions

- 1191
- 580
- 414
- 360
- 337
- 234
- 195
- 110
- 90
- 73



Caps

Input image

Output bottle cap art

Source: whitehouse.gov

New image processing problem

Optimization:
simulated annealing strategy

Related work



Color quantization
[Xiang 1997]



Halftoning
[Velho and Gomes 1991]

Related work



Color quantization
[Xiang 1997]



Halftoning
[Velho and Gomes 1991]



Pixel art
[Gerstner et al. 2013]

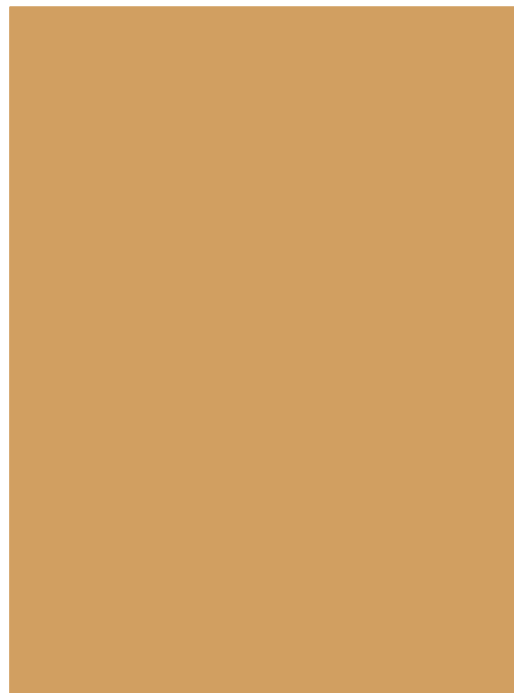
Problem setup



Input image

580 ●
414 ●
195 ○
360 ●
1191 ●
234 ○
337 ●
110 ●
90 ●
73 ●

Caps



Canvas

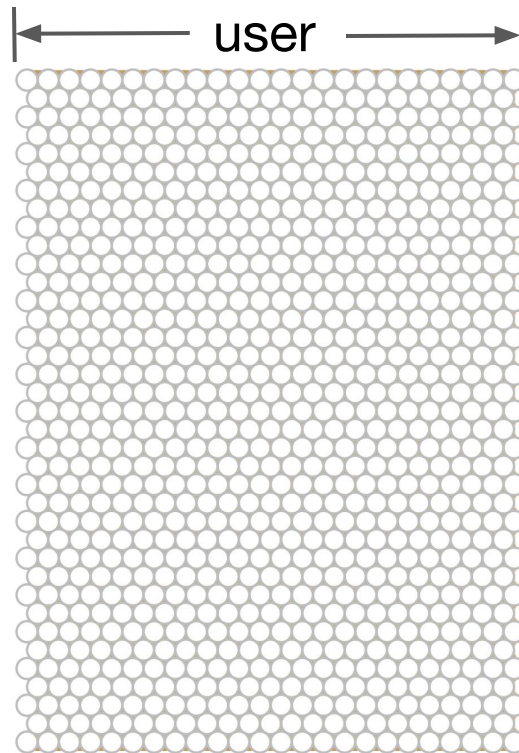
Problem setup



Input image

- 580 ●
- 414 ●
- 195 ○
- 360 ●
- 1191 ●
- 234 ○
- 337 ●
- 110 ●
- 90 ●
- 73 ●

Caps

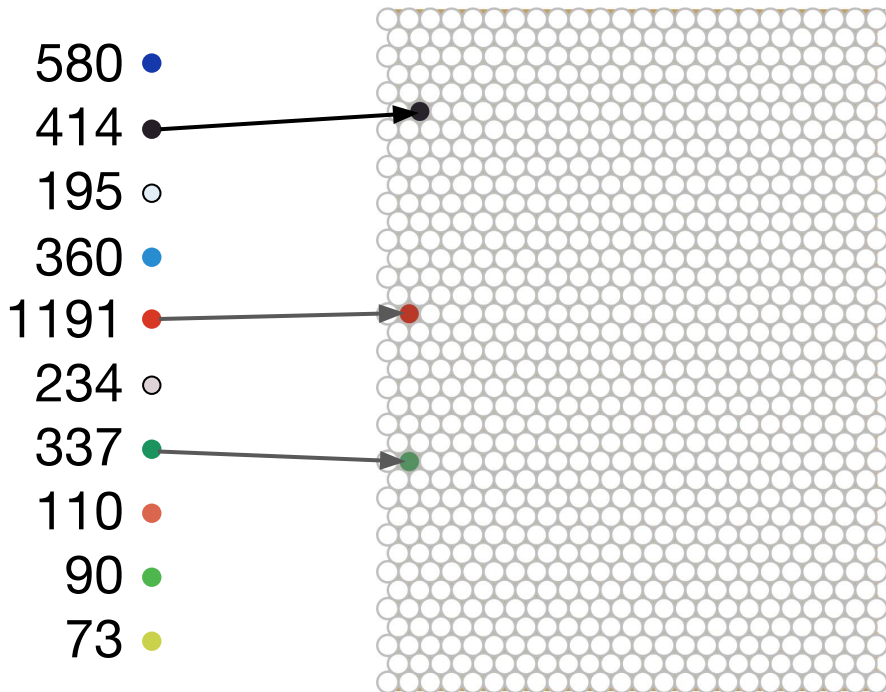


Bottle cap grid

Problem setup



Input image



Caps

Bottle cap grid

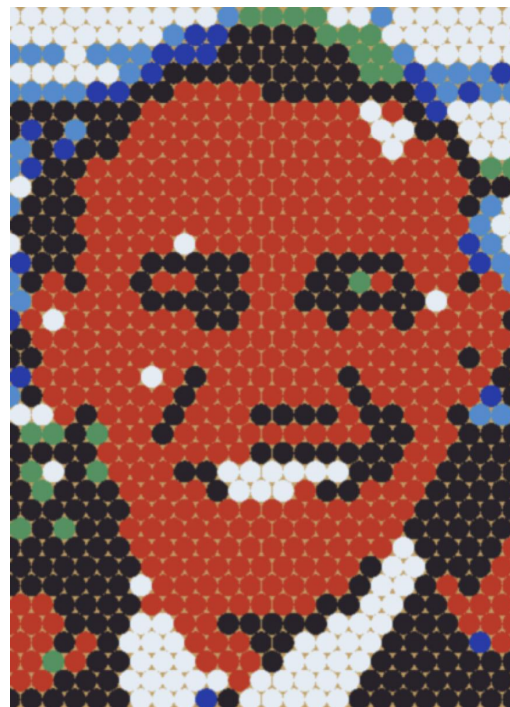
Problem setup



Input image

- 580 ●
- 414 ●
- 195 ○
- 360 ●
- 1191 ●
- 234 ○
- 337 ●
- 110 ●
- 90 ●
- 73 ●

Caps



Computer-generated
bottle cap art

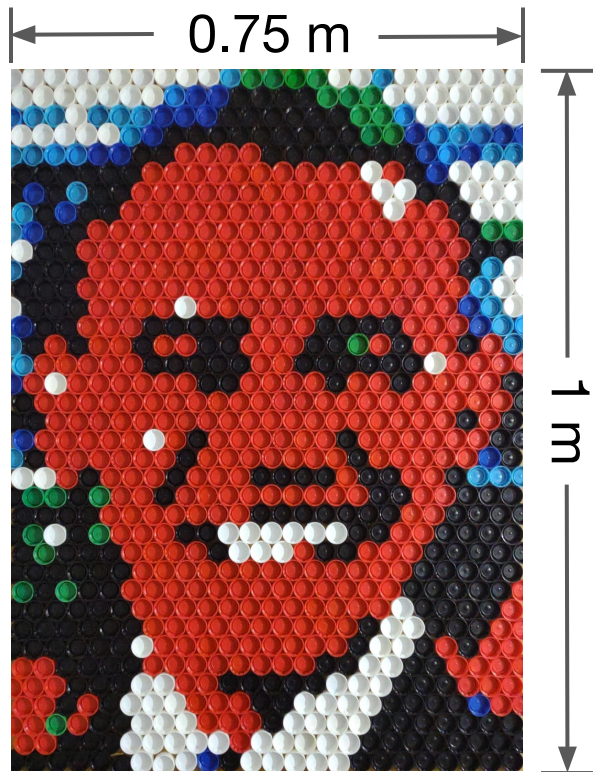
Problem setup



Input image

- 580 ●
- 414 ●
- 195 ○
- 360 ●
- 1191 ●
- 234 ○
- 337 ●
- 110 ●
- 90 ●
- 73 ●

Caps



Physically assembled
bottle cap art

Naive solution



Input image

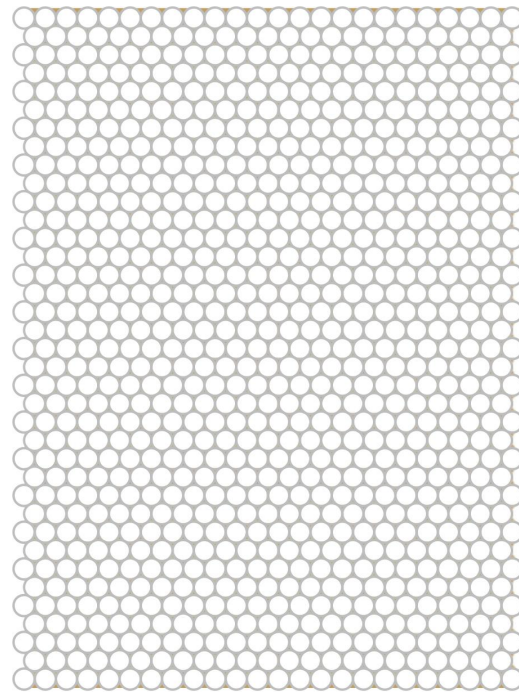


Naive solution

Spatial discretization



Full resolution input

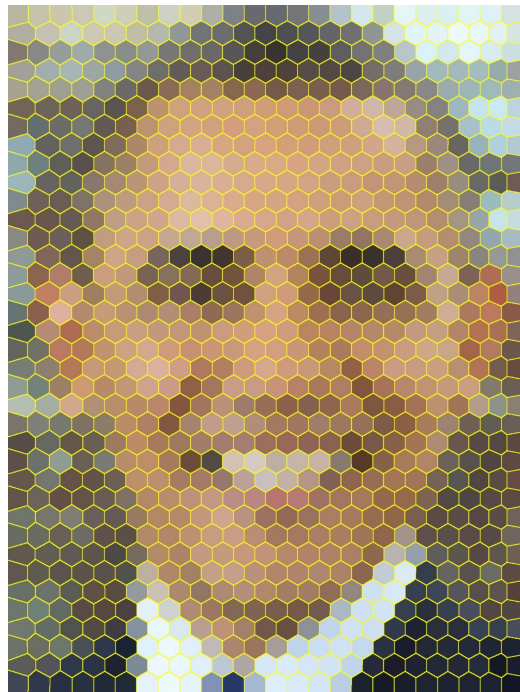


Bottle cap grid

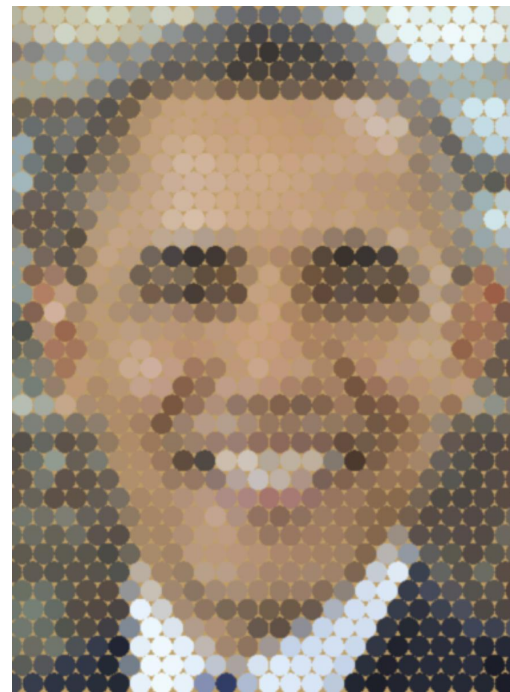
Spatial discretization



Full resolution input



Voronoi diagram



Discretization

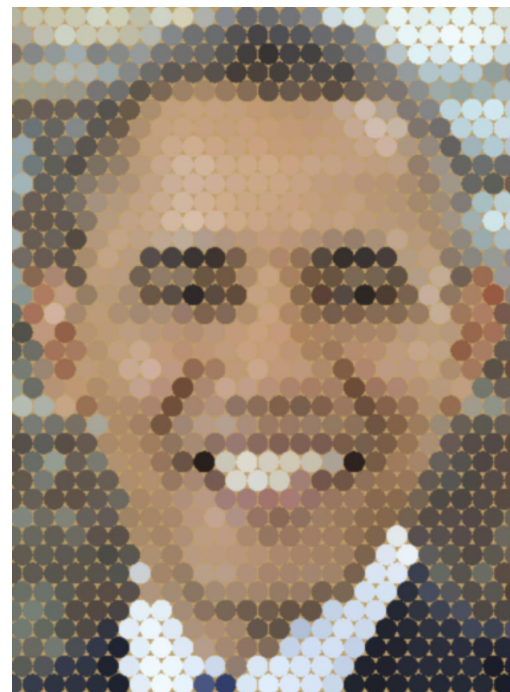
Spatial discretization



Full resolution input



SLIC with $\alpha=50$
[Achanta et al. 2012]



Discretization

Spatial discretization



Full resolution input



SLIC with $\alpha=5$
[Achanta et al. 2012]



Discretization

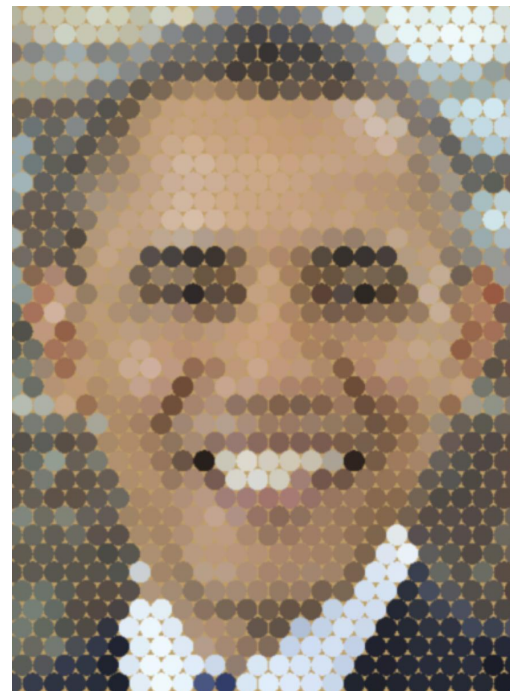
Spatial discretization



Full resolution input

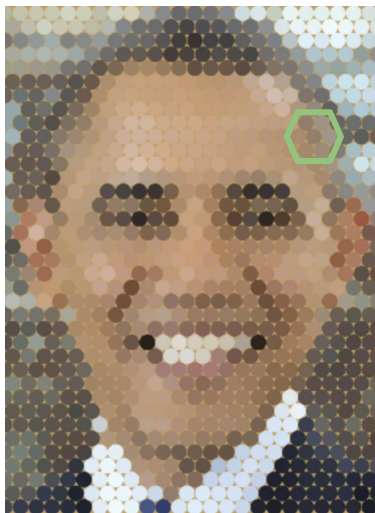


SLIC with $\alpha=50$
[Achanta et al. 2012]

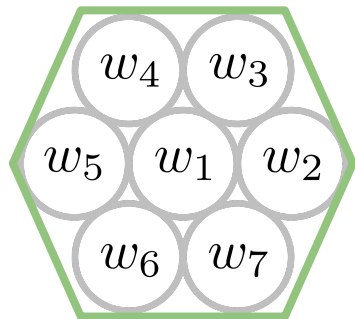


Reference image

Structural similarity



Reference **X**



Window and weights

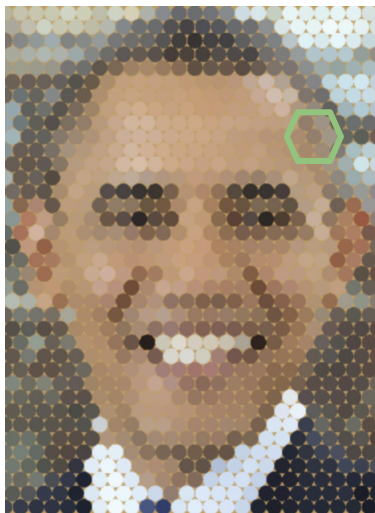
Local color mean

$$\mu_x = \sum_{i=1}^7 w_i \mathbf{x}_i$$

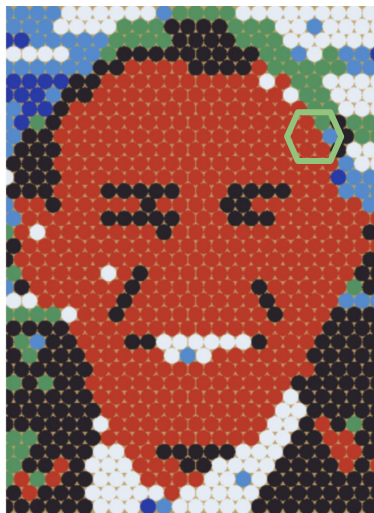
Local color deviation

$$\sigma_x = \left(\sum_{i=1}^7 w_i (\mathbf{x}_i - \mu_x) \right)^{\frac{1}{2}}$$

Structural similarity



Reference **X**



State **Y**

SSIM ≈ 0 

SSIM ≈ 1 

$$\mu_x = \sum_{i=1}^7 w_i \mathbf{x}_i \quad \sigma_x = \left(\sum_{i=1}^7 w_i (\mathbf{x}_i - \mu_x) \right)^{\frac{1}{2}}$$

$$\mu_y = \sum_{i=1}^7 w_i \mathbf{y}_i \quad \sigma_y = \left(\sum_{i=1}^7 w_i (\mathbf{y}_i - \mu_y) \right)^{\frac{1}{2}}$$

$$\sigma_{xy} = \sum_{i=1}^7 w_i (\mathbf{x}_i - \mu_x)(\mathbf{y}_i - \mu_y)$$

$$\text{SSIM} = \frac{(2\mu_x\mu_y + \gamma_1)}{(\mu_x^2 + \mu_y^2 + \gamma_1)} \cdot \frac{(2\sigma_{xy} + \gamma_2)}{(\sigma_x^2 + \sigma_y^2 + \gamma_2)}$$

Structural similarity



Reference **X**

SSIM ≈ 0 



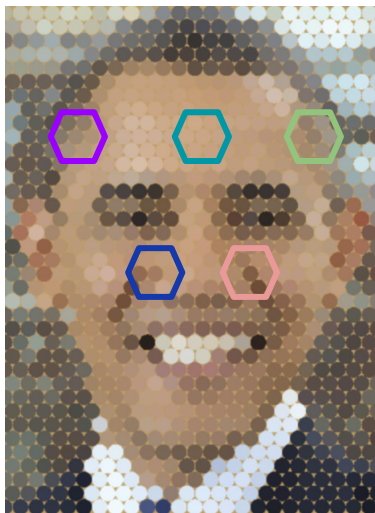
State **Y**

SSIM ≈ 1 

Loop over all windows

$$\text{MSSIM}(\mathbf{X}, \mathbf{Y}) = \frac{1}{M} \sum_{j=1}^M \text{SSIM}(\mathbf{X}_j, \mathbf{Y}_j)$$

Structural similarity



Reference **X**



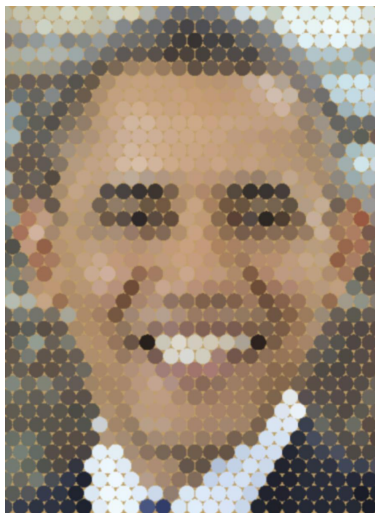
State **Y**

Our final energy

$$E(\mathbf{X}, \mathbf{Y}) = \frac{1}{M} \sum_{j=1}^M \text{SSIM}(\mathbf{X}_j, \mathbf{Y}_j) \cdot \text{Pen}(j)$$

has a penalty term to encourage constant regions in the reference to be constant in the result.

Optimization



Reference \mathbf{X}

●	1191
●	580
●	414
●	360
●	337
○	234
○	195
●	110
●	90
●	73

Caps

- Caps given by user

$$E(\mathbf{X}, \mathbf{Y}) = \frac{1}{M} \sum_{j=1}^M \text{SSIM}(\mathbf{X}_j, \mathbf{Y}_j) \cdot \text{Pen}(j)$$

Optimization



Reference **X**

●	1191
●	580
●	414
●	360
●	337
○	234
○	195
●	110
●	90
●	73

Caps

- Caps given by user
- Some cap colors are discarded as a preprocess

$$E(\mathbf{X}, \mathbf{Y}) = \frac{1}{M} \sum_{j=1}^M \text{SSIM}(\mathbf{X}_j, \mathbf{Y}_j) \cdot \text{Pen}(j)$$

Optimization



Reference \mathbf{X}

●	1191
●	580
●	414
●	360
●	337
○	234
○	195
●	110
●	90
●	73

Caps



Initial solution \mathbf{Y}_0

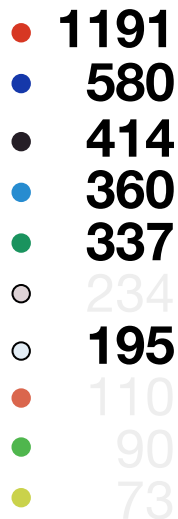
- Caps given by user
- Some cap colors are discarded as a preprocess
- Naive initial solution

$$E(\mathbf{X}, \mathbf{Y}) = \frac{1}{M} \sum_{j=1}^M \text{SSIM}(\mathbf{X}_j, \mathbf{Y}_j) \cdot \text{Pen}(j)$$

Optimization



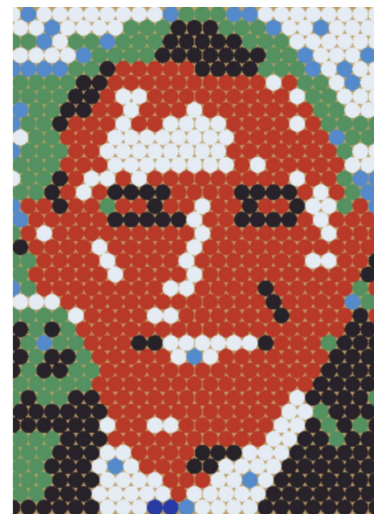
Reference X



Caps



Initial solution Y_0



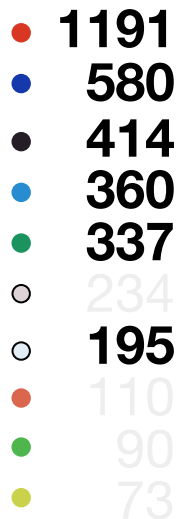
Intermediate Y

- Simulated annealing strategy
- Update neighborhood with a single color

Optimization



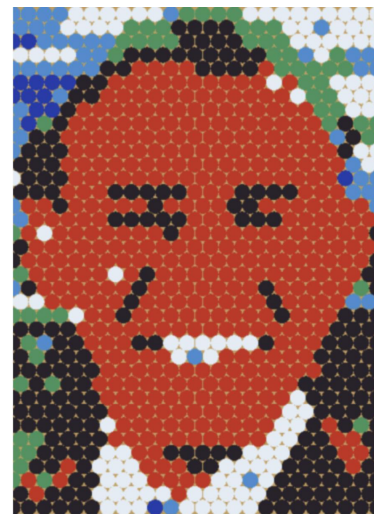
Reference **X**



Caps



Initial solution **Y₀**



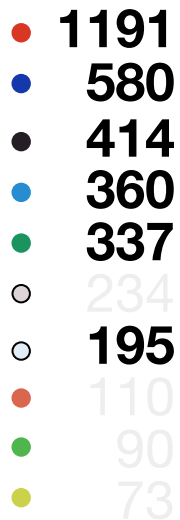
Intermediate **Y**

- Simulated annealing strategy
- Update neighborhood with a single color

Optimization



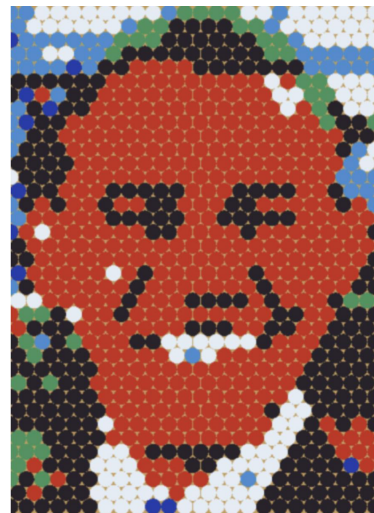
Reference X



Caps



Initial solution Y_0

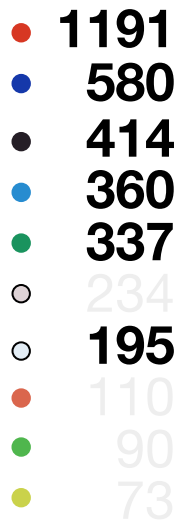


Intermediate Y

Optimization



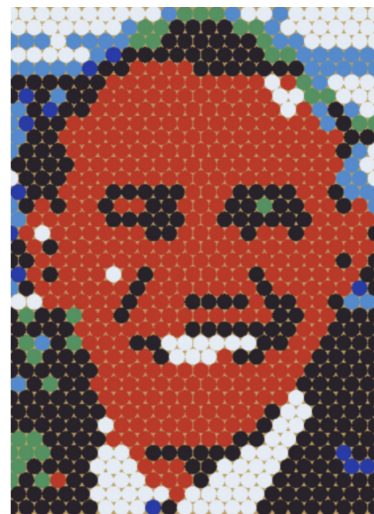
Reference X



Caps



Initial solution Y_0



Final result

Results

● 1191 ● 580 ● 414 ● 360 ● 337 ○ 234 ○ 195 ● 110 ● 90 ● 73



Input image

Girl with a Pearl Earring by
Johannes Vermeer

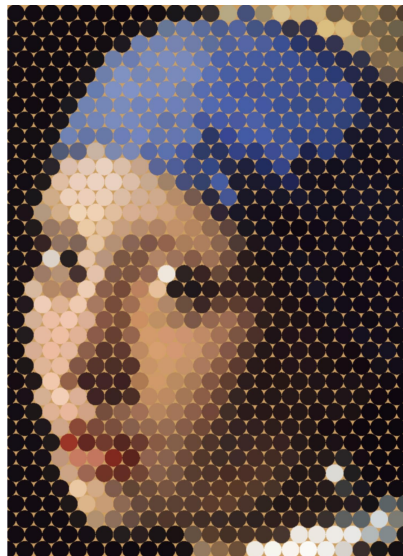
Results

● 1191 ● 580 ● 414 ● 360 ● 337 ○ 234 ○ 195 ● 110 ● 90 ● 73



Input image

Girl with a Pearl Earring by
Johannes Vermeer



Spatial
discretization

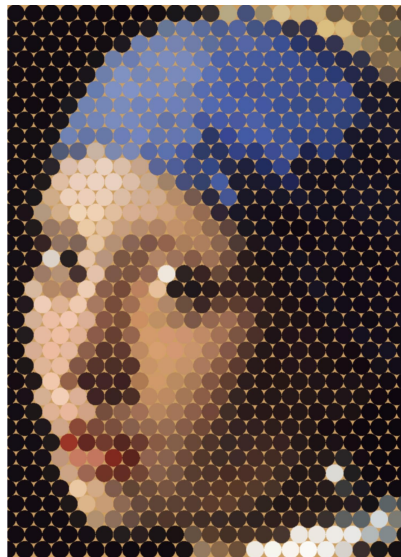
Results

● 1191 ● 580 ● 414 ● 360 ● 337 ○ 234 ○ 195 ● 110 ● 90 ● 73



Input image

Girl with a Pearl Earring by
Johannes Vermeer



Spatial
discretization



Initial solution

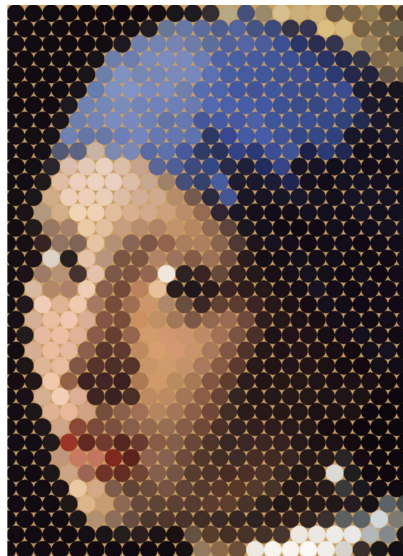
Results

● 1191 ● 580 ● 414 ● 360 ● 337 ○ 234 ○ 195 ● 110 ● 90 ● 73



Input image

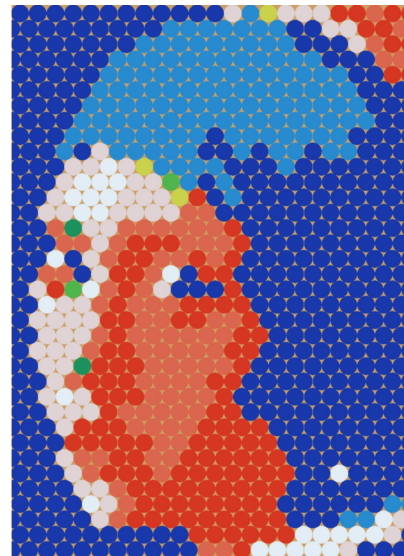
Girl with a Pearl Earring by
Johannes Vermeer



Spatial
discretization



Initial solution



Computer-
generated
bottle cap art

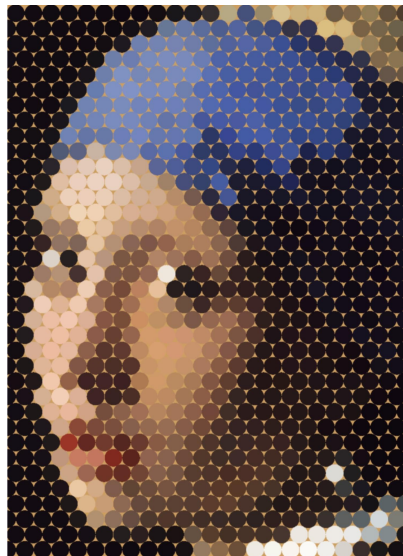
Results

● 1191 ● 580 ● 414 ● 360 ● 337 ○ 234 ○ 195 ● 110 ● 90 ● 73



Input image

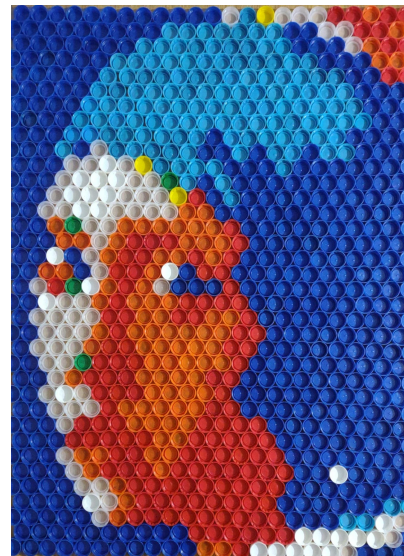
Girl with a Pearl Earring by
Johannes Vermeer



Spatial
discretization



Initial solution



Physically
assembled
bottle cap art

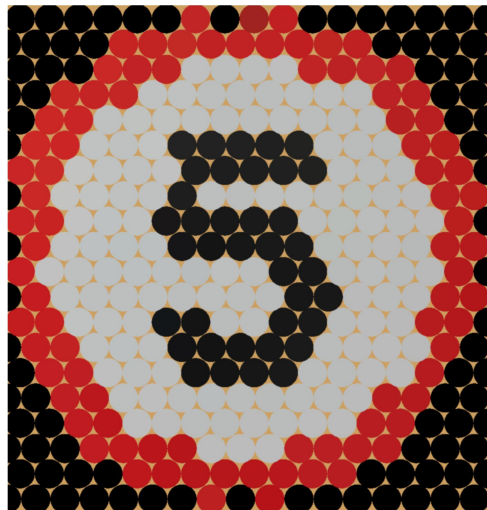
Results

● 1191 ● 580 ● 414 ● 360 ● 337 ○ 234 ○ 195 ● 110 ● 90 ● 73



Input image

By Flickr user zaphad1



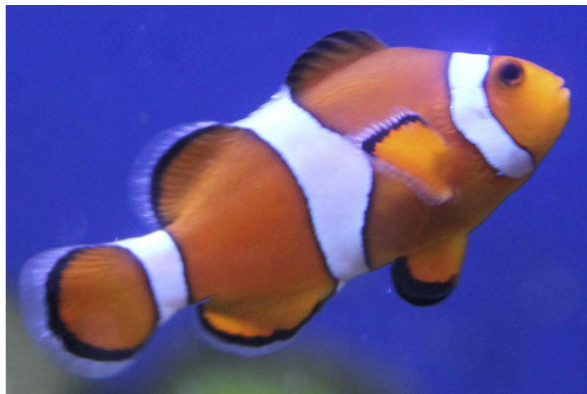
Spatial discretization



(Assembled)
initial/final
solution

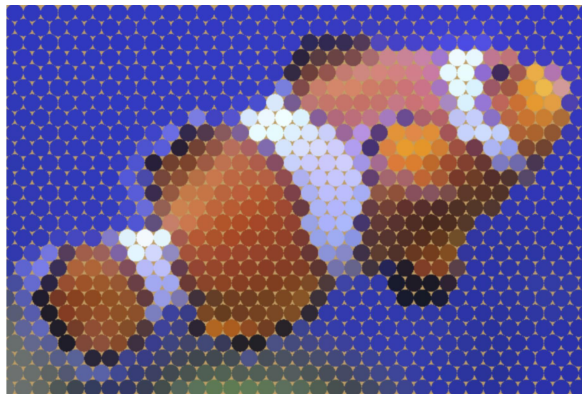
Results

● 1191 ● 580 ● 414 ● 360 ● 337 ○ 234 ○ 195 ● 110 ● 90 ● 73



Input image

By Flickr user Mike Sayre



Spatial discretization



Computer-generated
bottle cap art

Results

● 1191 ● 580 ● 414 ● 360 ● 337 ○ 234 ○ 195 ● 110 ● 90 ● 73



Input image

By Flickr user Christopher Gabbard



Spatial discretization



Physically assembled
bottle cap art

Pixel art methods

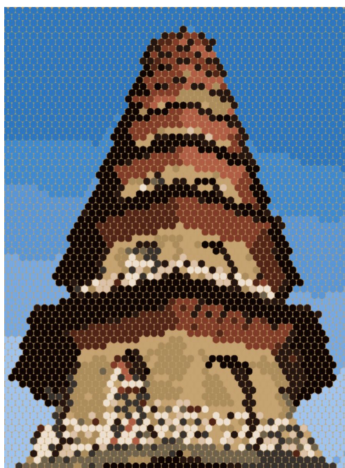
- 2000 ● 2000
- 2000 ● 2000
- 2000 ● 2000
- 2000 ● 2000
- 2000 ● 2000
- 2000 ● 2000
- 2000 ● 2000
- 2000 ● 2000

Caps

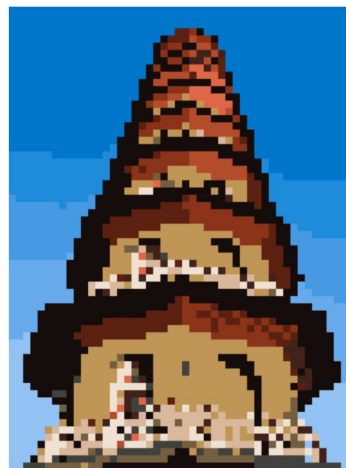


Input image

By Flickr user
William Warby



Our result



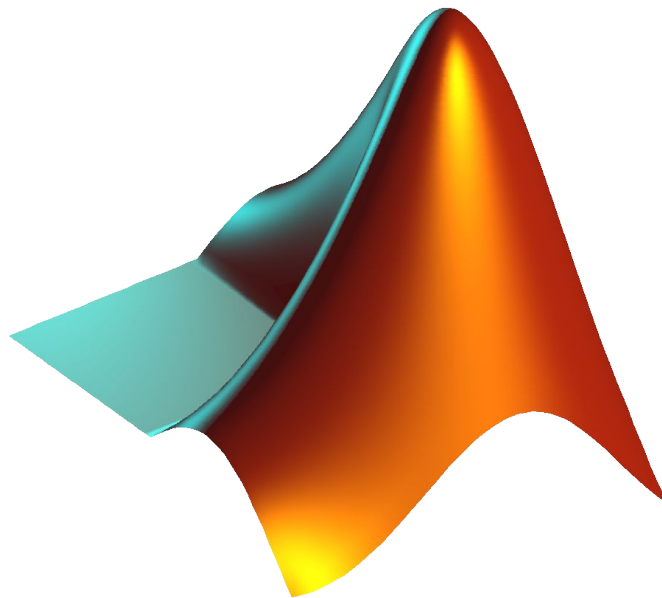
[Gerstner et
al. 2013]



[Kopf et al.
2013]

Implementation: Matlab program

- Modification of Matlab's `slic` built-in function
- Vectorization
- Re-use of local SSIM values



Matlab's logo (Mathworks)

Timings

	(Preprocessing)	(Optimization)	(Physical)
Result	Secs. 4.1 to 4.4	Section 4.5	Assembling
Figure 1	0.33 secs	192.97 secs	1h 45 min
Figure 2	0.31 secs	133.21 secs	1h 43 min
Figure 10	0.72 secs	129.51 secs	1h 43 min
Figure 11	0.72 secs	222.87 secs	1h 27 min
Figure 12	0.77 secs	18.58 secs	35 min
Figure 13	0.67 secs	83.77 secs	37 min

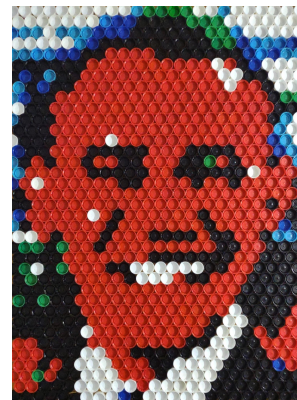


Figure 2

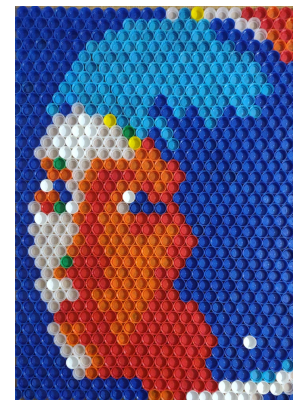


Figure 11

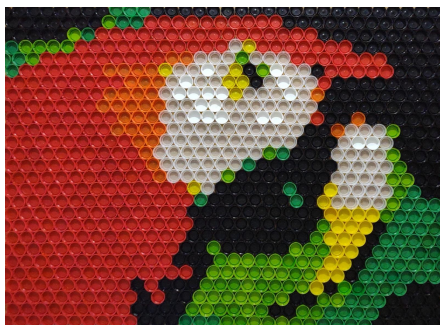


Figure 1



Figure 10



Figure 12

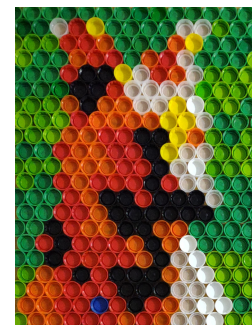


Figure 13

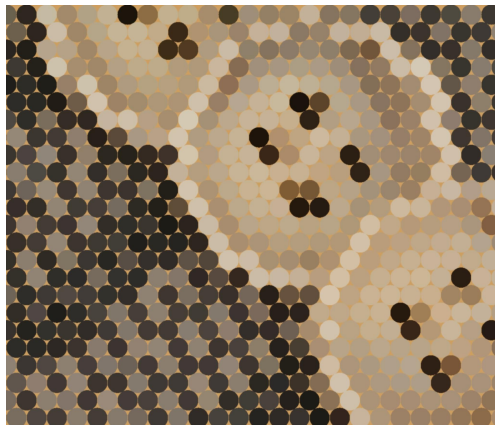
Limitation

● 1191 ● 580 ● 414 ● 360 ● 337 ○ 234 ○ 195 ● 110 ● 90 ● 73

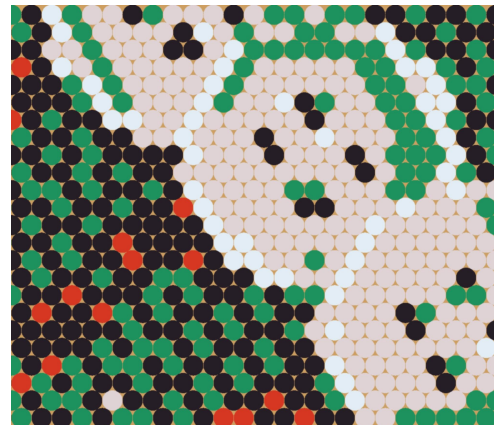


Input image

By Flickr user Clint Budd



Spatial discretization



Computer-generated
bottle cap art

Future works

- Faster optimization and run the method on image collections

(Optimization)

Section 4.5

192.97 secs

133.21 secs

129.51 secs

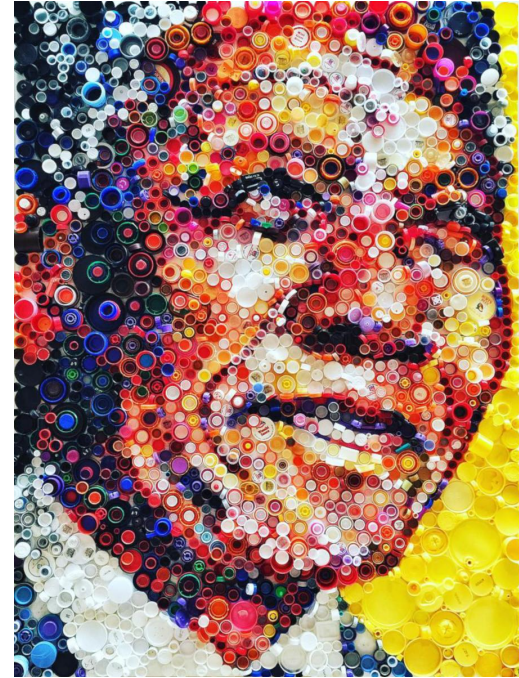
222.87 secs

18.58 secs

83.77 secs

Future works

- Faster optimization and run the method on image collections
- Other cap grids and cap sizes



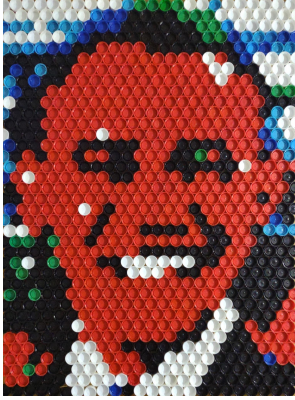
Mandela,
by artist Denise Hugues

Future works

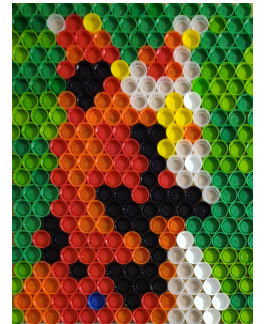
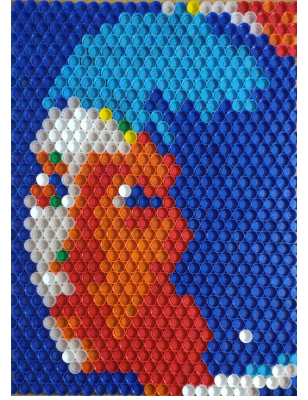
- Faster optimization and run the method on image collections
- Other cap grids and cap sizes
- Other graphics problems that use wasted material



Thank you!



For more, visit the website:
mtm.ufsc.br/~leo/bottle_cap_art/



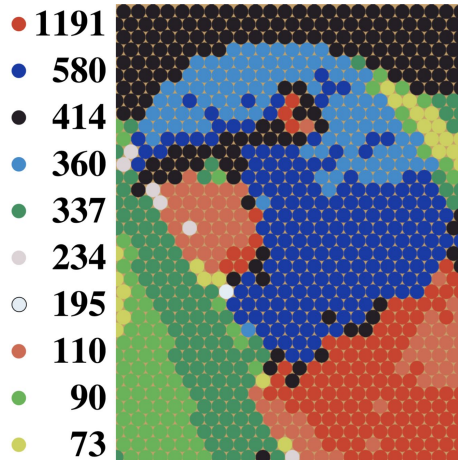
Backup slides

Varying sizes

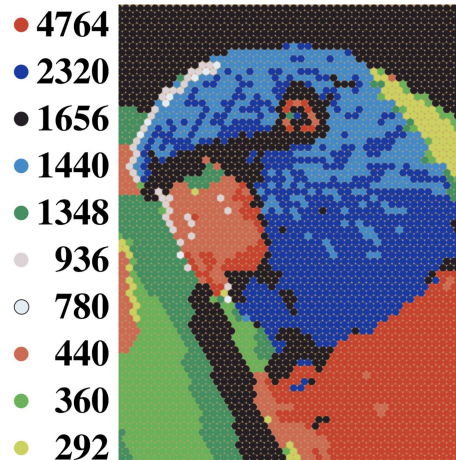


Input image

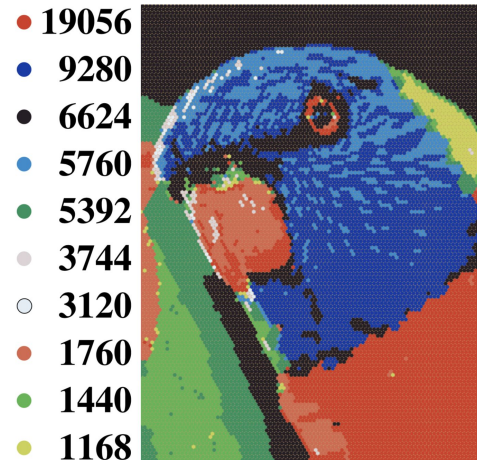
By Flickr user
troposa1



1 meter by
0.75 meters



2 meters by
1.5 meters

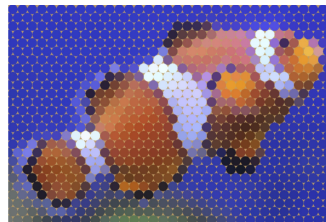


4 meters by
3 meters

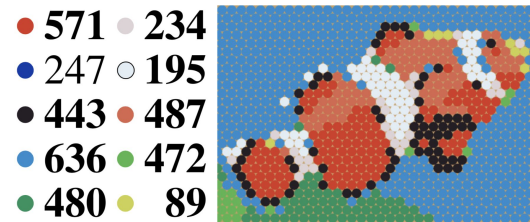
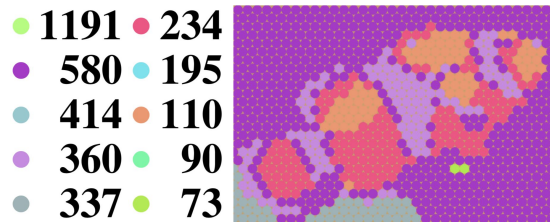
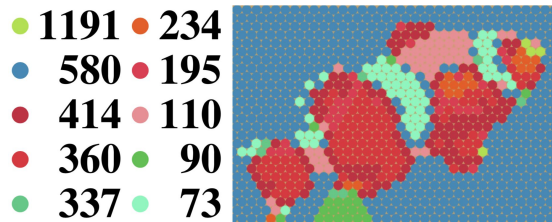
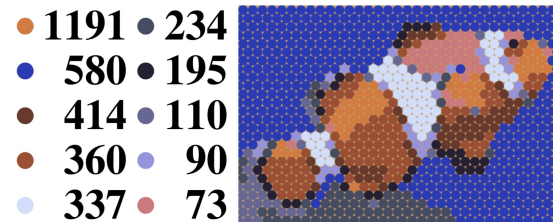
Other caps



Input image

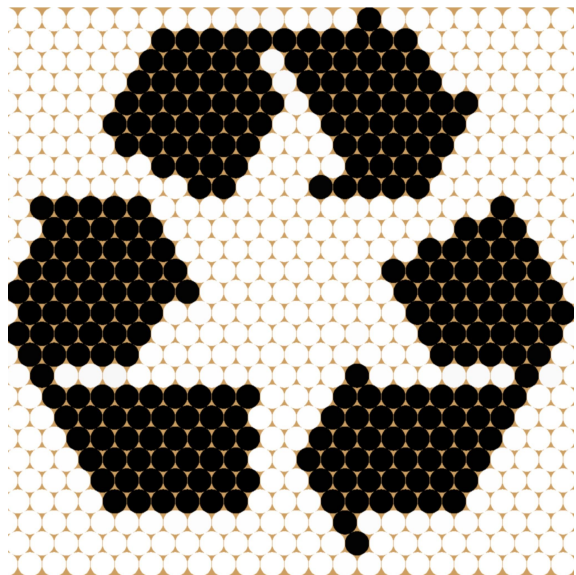


Discretization

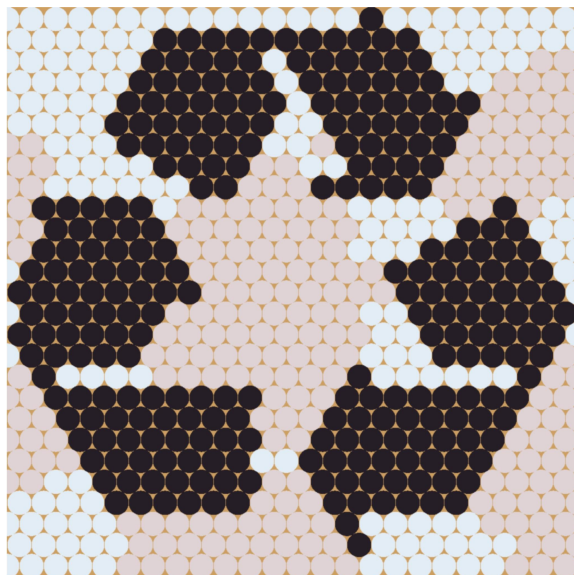


Caps preprocessing

● 1191 ● 580 ● 414 ● 360 ● 337 ○ 234 ○ 195 ● 110 ● 90 ● 73



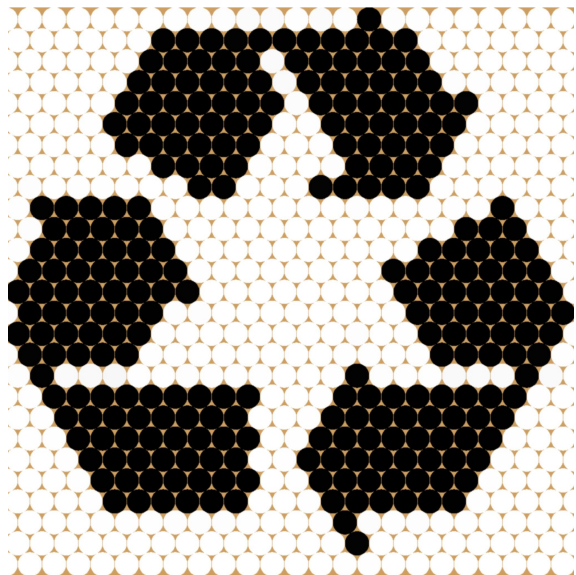
Spatial discretization



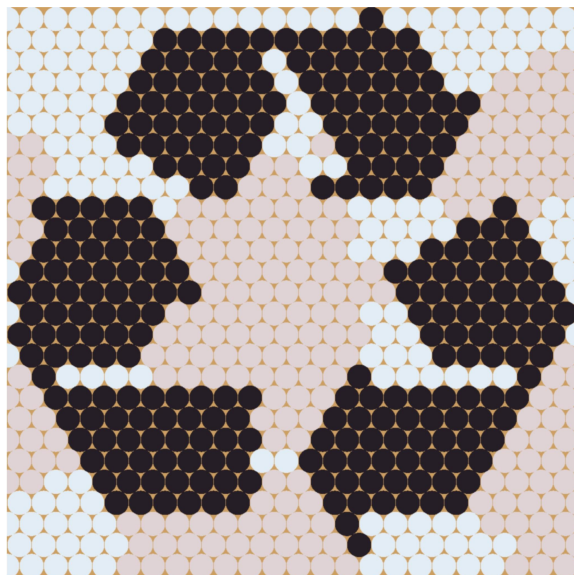
Result using all colors

Caps preprocessing

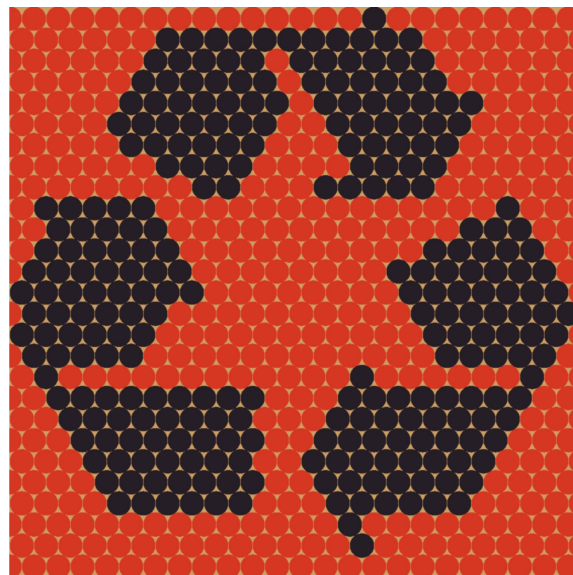
● 1191 ● 580 ● 414 ● 360 ● 337 ○ 234 ○ 195 ● 110 ● 90 ● 73



Spatial discretization



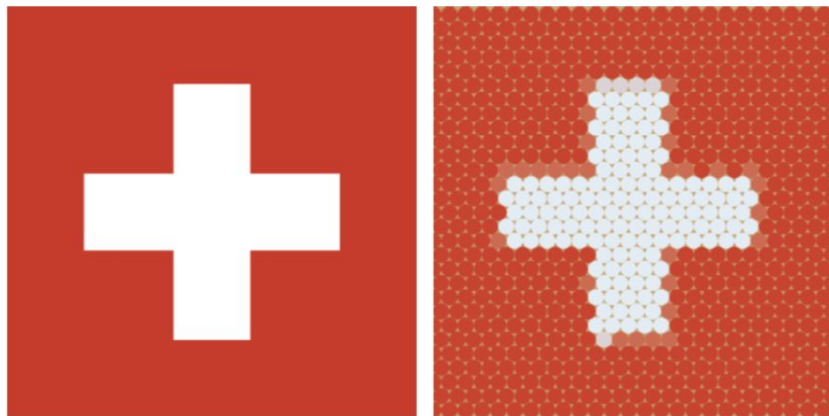
Result using all colors



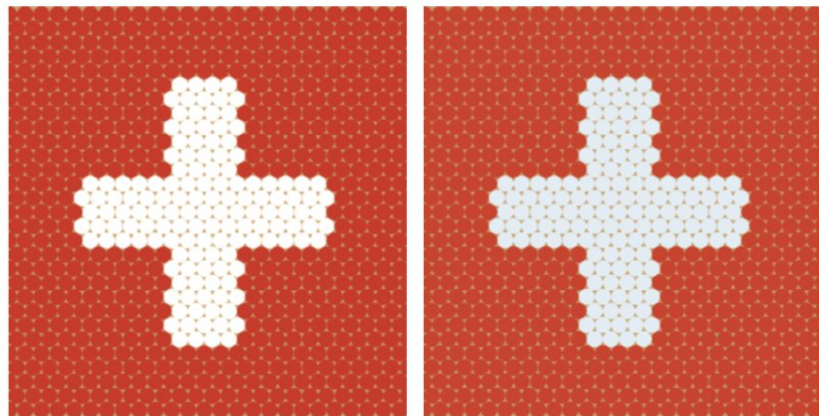
Result

Optimization with full and low resolution reference

● 1191 ● 580 ● 414 ● 360 ● 337 ○ 234 ○ 195 ● 110 ● 90 ● 73



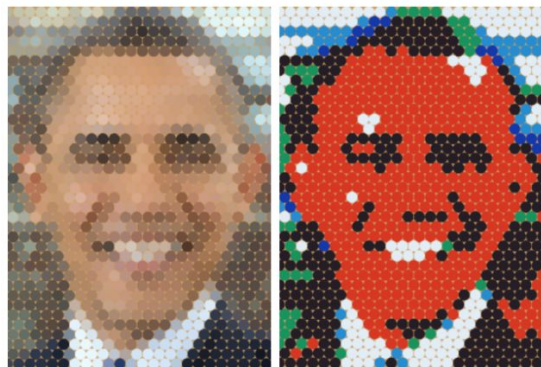
Optimization with
full resolution reference



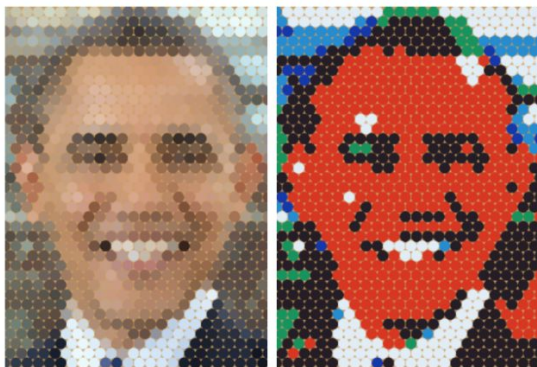
Optimization with
low resolution reference

Varying alpha

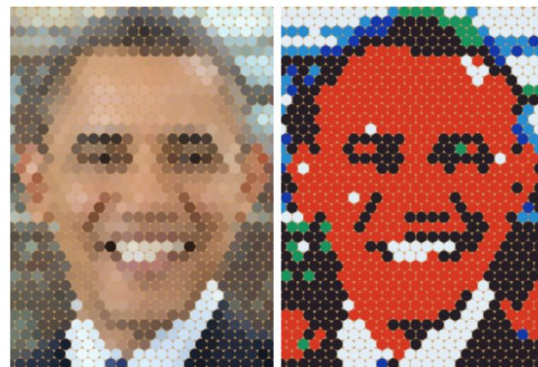
● 1191 ● 580 ● 414 ● 360 ● 337 ○ 234 ○ 195 ● 110 ● 90 ● 73



alpha = 500



alpha = 100



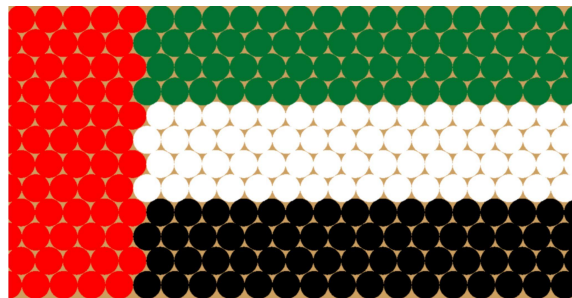
alpha = 50
(our choice)

Penalty term

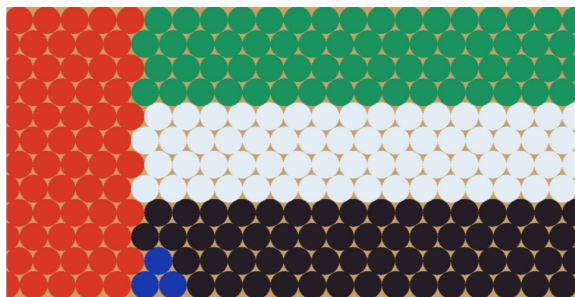
● 1191 ● 580 ● 414 ● 360 ● 337 ○ 234 ○ 195 ● 110 ● 90 ● 73



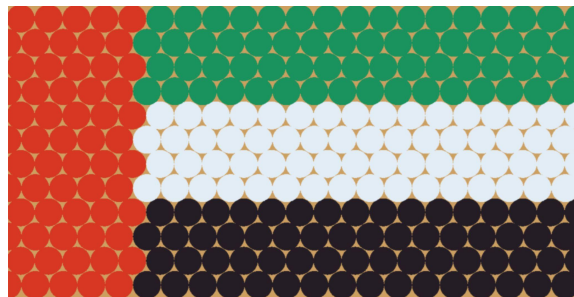
Input image



Spatial discretization



Result without penalty



Result with penalty