

- $Mdx + Ndy = 0$

Fator integrante dependente de x : $\frac{1}{N(x)} \left(\frac{\partial M}{\partial y} - \frac{\partial N}{\partial x} \right) \equiv f(x) \therefore F(x) = e^{\int f(x) dx}$.

Fator integrante dependente de y : $\frac{1}{M(x)} \left(\frac{\partial N}{\partial x} - \frac{\partial M}{\partial y} \right) \equiv g(y) \therefore F(y) = e^{\int g(y) dy}$.

- $y' + p(x)y = g(x)y^a \Rightarrow u(x) = y^{1-a}$

| $r(x)$ | y_p |
|--|---|
| $C_n X^n + C_{n-1} x^{n-1} + \dots + C_1 x + C_0$ | $A_n X^n + A_{n-1} x^{n-1} + \dots + A_1 x + A_0$ |
| $C e^{rx}$ | $A e^{rx}$ |
| $C \cos kx$ | $A \cos kx + B \sin kx$ |
| $C \sin kx$ | $A \cos kx + B \sin kx$ |
| $(C_n X^n + C_{n-1} x^{n-1} + \dots + C_1 x + C_0) e^{rx}$ | $(A_n X^n + A_{n-1} x^{n-1} + \dots + A_1 x + A_0) e^{rx}$ |
| $(C_n X^n + C_{n-1} x^{n-1} + \dots + C_1 x + C_0) \cos kx$ | $(A_n X^n + A_{n-1} x^{n-1} + \dots + A_1 x + A_0) \cos kx + (B_n X^n + B_{n-1} x^{n-1} + \dots + B_1 x + B_0) \sin kx$ |
| $(C_n X^n + C_{n-1} x^{n-1} + \dots + C_1 x + C_0) \sin kx$ | $(A_n X^n + A_{n-1} x^{n-1} + \dots + A_1 x + A_0) \cos kx + (B_n X^n + B_{n-1} x^{n-1} + \dots + B_1 x + B_0) \sin kx$ |
| $C e^{rx} \cos kx$ | $A e^{rx} \cos kx + B e^{rx} \sin kx$ |
| $C e^{rx} \sin kx$ | $A e^{rx} \cos kx + B e^{rx} \sin kx$ |
| $(C_n X^n + C_{n-1} x^{n-1} + \dots + C_1 x + C_0) e^{rx} \cos kx$ | $(A_n X^n + A_{n-1} x^{n-1} + \dots + A_1 x + A_0) e^{rx} \cos kx + (B_n X^n + B_{n-1} x^{n-1} + \dots + B_1 x + B_0) e^{rx} \sin kx$ |
| $(C_n X^n + C_{n-1} x^{n-1} + \dots + C_1 x + C_0) e^{rx} \sin kx$ | $(A_n X^n + A_{n-1} x^{n-1} + \dots + A_1 x + A_0) e^{rx} \cos kx + (B_n X^n + B_{n-1} x^{n-1} + \dots + B_1 x + B_0) e^{rx} \sin kx$ |

- $y_h = C_1 y_1 + C_2 y_2 \quad y_p = u y_1 + v y_2$

$$u = - \int \frac{r(x)y_2}{W(y_1, y_2)} dx \quad v = \int \frac{r(x)y_1}{W(y_1, y_2)} dx$$