

(33 - cont.)

$$= \cos^2 x \sin^2 x + \cos^6 x - \sin^4 x - \sin^2 x$$

$$+ 2 \sin^4 x - \sin^6 x$$

$$= (\cos^2 x - 1) \sin^2 x + \cos^6 x + \sin^4 x$$

$$- \sin^6 x$$

$$= -\sin^2 x \sin^2 x + \cos^6 x + \sin^4 x - \sin^6 x$$

$$= -\cancel{\sin^4 x} + \cos^6 x + \cancel{\sin^4 x} - \sin^6 x$$

$$= \underline{\underline{\cos^6 x - \sin^6 x}}$$

Another derivation :

$$\cos^6 x - \sin^6 x = (\cos^2 x)^3 - (\sin^2 x)^3$$

$$\left. \begin{aligned} a^3 - b^3 &= (a-b)(a^2 + ab + b^2) \\ a^3 + b^3 &= (a+b)(a^2 - ab + b^2) \end{aligned} \right\} = (\cos^2 x - \sin^2 x) (\cos^4 x + \cos^2 x \sin^2 x + \sin^4 x)$$

$$= \cos 2x \cdot \left((\cos^2 x + \sin^2 x)^2 - \cos^2 x \sin^2 x \right)$$

$$= \cos 2x \cdot \left(1 - \cos^2 x \sin^2 x \right)$$

$$= \cos 2x \left(1 - \frac{1}{4} \sin^2 2x \right) //$$