

$$36) \frac{\sin 2x}{1 + \cos 2x} \cdot \frac{\cos x}{1 + \cos x} = \operatorname{tg} \frac{x}{2}$$

$$\begin{aligned} \rightarrow // \frac{\sin 2x}{1 + \cos 2x} \cdot \frac{\cos x}{1 + \cos x} &= \frac{2 \sin x \cos x}{1 + (2 \cos^2 x - 1)} \cdot \frac{\cos x}{1 + \cos x} \\ &= \frac{\cancel{2} \sin x \cos x}{\cancel{2} \cos^2 x} \cdot \frac{\cos x}{1 + \cos x} \\ &= \frac{\sin x}{1 + \cos x} = \frac{2 \sin \frac{x}{2} \cos \frac{x}{2}}{1 + (2 \cos^2 \frac{x}{2} - 1)} \\ &= \frac{\cancel{2} \sin \frac{x}{2} \cos \frac{x}{2}}{\cancel{2} \cos^2 \frac{x}{2}} = \frac{\sin \frac{x}{2}}{\cos \frac{x}{2}} \\ &= \operatorname{tg} \frac{x}{2} // \end{aligned}$$

$$37) \sin^2 x + \cos^4 x = \cos^2 x + \sin^4 x$$

$$\begin{aligned} \rightarrow // \sin^2 x + \cos^4 x &= \sin^2 x + (\cos^2 x)^2 \\ &= \sin^2 x + (1 - \sin^2 x)^2 \\ &= \sin^2 x + 1 - 2 \sin^2 x + \sin^4 x \\ &= \underbrace{1 - \sin^2 x} + \sin^4 x \\ &= \cos^2 x + \sin^4 x // \end{aligned}$$